

Coded Spatial Modulation applied to Optical Wireless Communications in Indoor Environments

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Abstract—Spatial Modulation (SM) is a combined multiple-input-multiple-output (MIMO) and digital modulation technique which besides common signal modulation conveys additional information bits in the spatial domain. To this end, only one transmitter is active at any time instance. The actual index of each emitter represents a unique spatial constellation point and thus conveys additional information. As a consequence, SM completely avoids inter-channel interference (ICI) and provides low detection complexity. Like for any MIMO scheme, the performance of SM is degraded in the presence of high channel correlation. Therefore, Trellis Coded Spatial Modulation (TCSM) applies coding techniques to the bits conveyed in the spatial domain to assist the detection of the active transmitter. As optical wireless communications (OWC) in indoor environments is subject to high spatial correlation and low channel distinctness, we evaluate the performance of coded SM applied to indoor OWC. For this purpose, we propose an enhanced coded SM technique which jointly encodes the bits conveyed in the signal and spatial domains. It is found in this paper that our enhanced coded SM technique can achieve gains in signal to noise ratio (SNR) of about 1 – 3 dB compared to the originally proposed TCSM scheme.

Index Terms—coding, MIMO, optical wireless communications, spatial modulation.

I. INTRODUCTION

Due to recent advances in solid-state lighting and the associated availability of frequency spectrum of hundreds of THz, optical wireless communications (OWC) has attracted attention for indoor data transmission as a promising complement to existing radio frequency (RF) systems [1]. Commonly for OWC, incoherent light sources are used as they enable the use of simple low cost optical devices. As a consequence, optical systems are mostly based on intensity modulation (IM) and direct detection (DD) by employing light emitting diodes (LEDs) as emitters and photo diodes as receivers, thus not providing phase information in the received signals [2]. Since there is an increasing adoption of LED lighting in homes and offices, this has fueled research that aims at using these devices not only for illumination but also for wireless communications [3]. Moreover, as there typically are several LEDs in an entire LED cluster, these multiple emitters can be used for data transmission. This inherently provides the essential prerequisite for the use of multiple-input-multiple-output (MIMO) techniques in conjunction with

OWC [4]. MIMO techniques are already widely used in RF communications to enhance the system performance as they increase the link reliability and provide high data rates [5].

Recently, Spatial Modulation (SM) has been proposed as a combined MIMO and digital modulation technique [6]. In addition to applying basic signal modulation, SM transmits additional bits in the spatial domain by considering the transmitter array as an extended constellation diagram. As only one transmitter is emitting a digitally modulated signal at any time instance, the index of this transmitter represents additional data bits. It has been shown that SM can outperform other MIMO schemes like Repetition Coding (RC) [7] and spatial multiplexing [6], while even providing lower computational complexity.

Like for any MIMO technique, the performance of SM is related to the channel characteristics. As a consequence, its performance is degraded in scenarios with high link correlation and low channel distinctness. Therefore, Trellis Coded Spatial Modulation (TCSM) has been proposed to improve the performance of SM over correlated channels [8], [9]. TCSM applies coding to the bits conveyed in the transmitter index in order to increase the free distance between sequences of spatial constellation points. Consequently, the transmitter detection is made more robust and the error ratio is reduced. In order to achieve these gains, TCSM splits the data bits into two subsets. The first subset directly specifies the digitally modulated signal to be emitted, whereas the second subset is first passed to an encoder and then used to determine the emitter to be activated. Consequently, TCSM differentiates between the bits represented by digital signal modulation and the bits conveyed in the spatial domain. However, this approach disallows a joint decoding at the receiver side, thus not allowing the full exploitation of the SM principle.

Therefore, in this paper we extend the TCSM technique to an enhanced coded SM scheme which jointly encodes the bits conveyed in the spatial as well as in the signal domain. To this end, a convolutional encoder is applied to all data bits *before* they are split into the two subsets which determine the digitally modulated signal and the active transmitter. It is found that our jointly encoding achieves higher coding gains than the originally proposed TCSM scheme if applied to OWC.

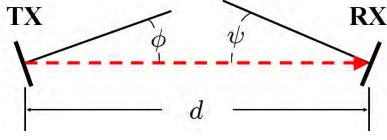


Fig. 2. Geometric scenario used for calculation of channel coefficients.

power). Moreover, r denotes the optical-to-electrical conversion coefficient and A is the detector area of the receiver. The distance between transmitter and receiver is depicted by d . As illustrated in Fig. 2, ϕ is the angle of emergence with respect to the transmitter (TX) axis and ψ is the angle of incidence with respect to the receiver (RX) axis. Consequently, the channel gain h_{n_r, n_t} depends on the position of both transmitter n_t and receiver n_r , *i.e.* their distance and angular alignment. Due to the use of SM, only one transmitter is emitting at any time instance and given independent identically distributed (i.i.d.) ones and zeros as data bits, each transmitter is activated with equal probability. Therefore, the average electrical power collected at each receiver is denoted by

$$E_{\text{RX}} = \left(\frac{1}{N_r} \frac{1}{N_t} \sum_{n_r=1}^{N_r} \sum_{n_t=1}^{N_t} h_{n_r, n_t} I \right)^2.$$

Without loss of generality, the performance of the evaluated SM schemes is studied using practical system parameters as follows: we analyse the channel gains of a setup which employs an off-the-shelf DL-6147-040 diode [11] at the transmitter side with $\Phi_{\frac{1}{2}} \approx 8^\circ$ and a wavelength of 658 nm. The optical receiver consists of a circuitry applying a BPX 61 Silicon PIN (positive intrinsic negative) photo diode [12] with an optical-to-electrical conversion coefficient of $r \approx 0.434$ A/W at 658 nm, a detector area of $A \approx 7$ mm² and $\Psi_{\frac{1}{2}} \approx 55^\circ$. The 3 dB cut-off frequency of the photo diode is about 17 MHz.

Fig. 3 displays an arbitrary optical wireless test setup which is used for channel measurements employing the diodes given above. As illustrated, the setup consists of two identical transmitters TX₁ and TX₂ which have a directed LOS connection towards the receiver. The spacing of the two transmitters is fixed to be 30 cm while their distance to the receiver d_1 , respectively d_2 , is varied. Both transmitters are oriented towards the receiver so that $\phi_1 = \phi_2 = 0$. As TX₁ is directly placed on the receiver axis, $\psi_1 = 0$ holds. However, TX₂ has an angular misalignment ψ_2 with respect to the receiver axis. Fig. 4 shows the measured channel gains for two scenarios,

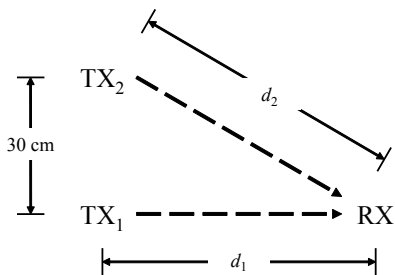
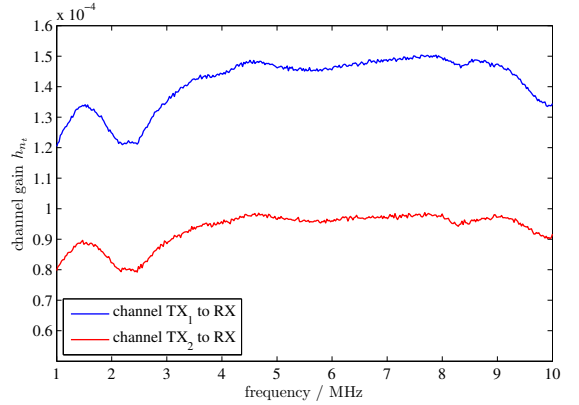
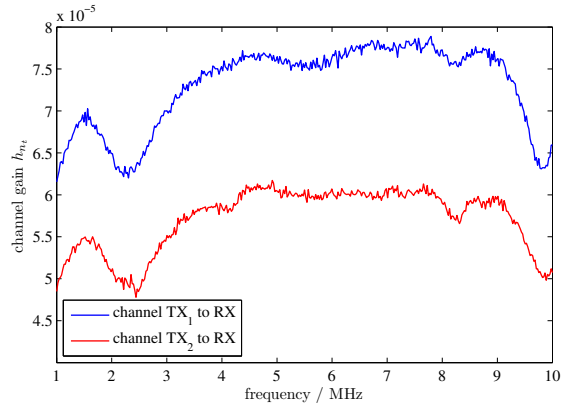


Fig. 3. Illustration of the optical wireless test setup.



(a) channel gains for $d_1 = 50$ cm and $d_2 \approx 58$ cm.



(b) channel gains for $d_1 = 70$ cm and $d_2 \approx 76$ cm.

Fig. 4. Measured gains of the optical wireless channels within the test setup.

similar to the setup presented in [13]. The gains are plotted for a frequency range of 1 – 10 MHz. For scenario 4(a), $d_1 = 50$ cm, $d_2 \approx 58$ cm and $\psi_2 \approx 31^\circ$. For scenario 4(b), $d_1 = 70$ cm, $d_2 \approx 76$ cm and $\psi_2 \approx 23^\circ$. The measurements show that the links are highly correlated and differ only by their absolute gain, due to the larger distance and angular misalignment of TX₂. Consequently, the gains have a time averaged correlation coefficient of

$$\rho(h_1, h_2) = \frac{E\{(h_1 - E\{h_1\})(h_2 - E\{h_2\})\}}{\sqrt{\text{VAR}\{h_1\} \text{VAR}\{h_2\}}} \approx 0.97,$$

with $E\{\cdot\}$ denoting the expectation operator and $\text{VAR}\{\cdot\}$ being the variance operator. Moreover, the measured optical channels show only little variations within the considered frequency range as their maximum coefficient of variation, $v_n = \sqrt{\text{VAR}\{h_n\}}/E\{h_n\}$, is only about 0.07. Therefore, the links can be represented by flat AWGN channels with constant attenuation. Table I displays the mean measured channel gains \bar{h}_n and the theoretical channel gains h_n for scenario 4(a) and 4(b). Moreover, the relative difference, $\Delta_n = 100 |\bar{h}_n - h_n|/h_n$, between the measured gains and the theoretical values is given. As the maximum difference is only about 6.49 %, the measured channel gains and the gains calculated using the geometrical model closely match.

TABLE I
COMPARISON OF MEASURED AND THEORETICAL CHANNEL GAINS.

	scenario 4(a)	scenario 4(b)
theoretical gain	$h_1 \approx 139.01 \cdot 10^{-6}$	$h_1 \approx 70.93 \cdot 10^{-6}$
	$h_2 \approx 87.65 \cdot 10^{-6}$	$h_2 \approx 55.07 \cdot 10^{-6}$
measured gain	$\bar{h}_1 \approx 141.59 \cdot 10^{-6}$	$\bar{h}_1 \approx 73.05 \cdot 10^{-6}$
	$\bar{h}_2 \approx 93.34 \cdot 10^{-6}$	$\bar{h}_2 \approx 57.17 \cdot 10^{-6}$
relative difference	$\Delta_1 \approx 1.86 \%$	$\Delta_1 \approx 2.99 \%$
	$\Delta_2 \approx 6.49 \%$	$\Delta_2 \approx 3.81 \%$

Therefore, we use this model in the following to derive the channel gains of different indoor setup scenarios. To this end, we consider a generic 4×4 indoor scenario ($N_r = 4$ and $N_t = 4$), which is located within a $4.0 \text{ m} \times 4.0 \text{ m} \times 3.0 \text{ m}$ room. We assume that the transmitters are placed at a height of $z = 3.00 \text{ m}$ and are oriented downwards to point straight down from the ceiling. The receivers are located at a height of $z = 0.75 \text{ m}$ (e.g. height of a table) and are oriented upwards to point straight up at the ceiling. Both transmitters and receivers are aligned in a quadratically 2×2 array which is centered in the middle of the room. On the basis of this scenario, we investigate different static setups with varying element spacings of the single transmitters on the x - and y -axis, depicted by d_{TX} , while the element spacing of the receivers is assumed to be 0.1 m on the x - and y -axis for all considered setups. This receiver spacing is chosen with regard to a practical implementation within a potential (hand-held) user device. Fig. 5 exemplarily shows the positioning of the 4×4 setup, at which the receivers are displayed as dots and the transmitters as triangular. The plotted cones illustrate the orientation of the transmit beams and the orientation of the receiver FOV. Applying (6) to this setup with $d_{\text{TX}} = 0.3 \text{ m}$, 0.5 m and 0.7 m , results in the following channel matrices:

$$\begin{aligned}
 \mathbf{H}_{d_{\text{TX}}=0.3} &\approx 10^{-5} \begin{pmatrix} 0.5934 & 0.4775 & 0.4775 & 0.3847 \\ 0.4775 & 0.5934 & 0.3847 & 0.4775 \\ 0.4775 & 0.3847 & 0.5934 & 0.4775 \\ 0.3847 & 0.4775 & 0.4775 & 0.5934 \end{pmatrix}, \\
 \mathbf{H}_{d_{\text{TX}}=0.5} &\approx 10^{-5} \begin{pmatrix} 0.3847 & 0.2691 & 0.2691 & 0.1889 \\ 0.2691 & 0.3847 & 0.1889 & 0.2691 \\ 0.2691 & 0.1889 & 0.3847 & 0.2691 \\ 0.1889 & 0.2691 & 0.2691 & 0.3847 \end{pmatrix}, \\
 \mathbf{H}_{d_{\text{TX}}=0.7} &\approx 10^{-5} \begin{pmatrix} 0.1889 & 0.1157 & 0.1157 & 0.0713 \\ 0.1157 & 0.1889 & 0.0713 & 0.1157 \\ 0.1157 & 0.0713 & 0.1889 & 0.1157 \\ 0.0713 & 0.1157 & 0.1157 & 0.1889 \end{pmatrix}.
 \end{aligned} \tag{7}$$

It can be seen that the symmetrical arrangement of the transmitters and receivers leads to equal channel gains for the wireless links with the same alignment, e.g. $h_{n_r n_t} = h_{n_t n_r}$. Moreover, if the spacing d_{TX} between the transmitters is small, the gains are quite similar, whereas if d_{TX} gets larger, the differences between the links increase due to the geometry of the setup scenario, i.e. the enlarged angular misalignment.

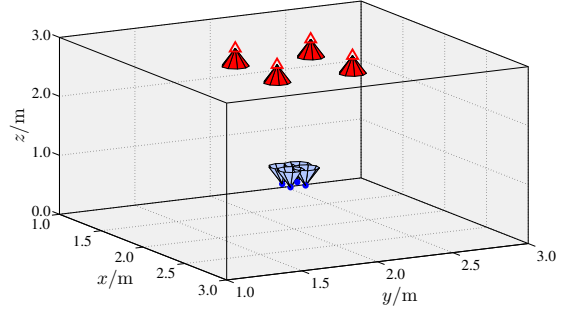


Fig. 5. Positioning of 4×4 setup with $d_{\text{TX}} = 0.5 \text{ m}$ within room.

IV. BIT ERROR RATIO PERFORMANCE OF CODED SPATIAL MODULATION

In the following, we evaluate the BER performance of coded SM applied to the optical wireless setup presented above. For encoding at the transmitter side, we assume a convolutional encoder with an octal presentation of $(161, 133)$, a coding rate of $c = \frac{1}{2}$, a constraint length of $l = 7$ and a free distance of $d_{\text{free}} = 10$. Furthermore, the encoded bits are additionally interleaved by a random block interleaver. As proposed in [8], [9], by applying TCSM, only the bits which determine the transmitter index are passed to the convolutional encoder, while the bits denoting the digitally modulated signal to be transmitted remain uncoded and are directly passed to the SM mapper (see Fig. 1 (b)). The encoded and interleaved bits are then used to determine the emitter which is activated according to the standard SM transmission scheme. In contrast, our proposed enhanced coded SM scheme passes *all* information bits to the convolutional encoder. The encoded bits are also interleaved and then passed to the standard SM mapper which maps them to the signal constellation points and transmitter indices as depicted in Fig. 1 (c). Note that for the sake of comparison, both coded SM schemes use the same $(161, 133)$ convolutional encoder. At the receiver side, the encoded bits of both coded SM schemes are deinterleaved and processed by a soft decision Viterbi decoder which has a traceback length of five times the constraint length.

Fig. 6 shows the BER performance of our enhanced coded SM scheme, TCSM and uncoded SM for a spectral efficiency of $R = 2 \text{ bit/s/Hz}$ in the considered 4×4 setup with different transmitter spacings of $d_{\text{TX}} = 0.3 \text{ m}$, 0.5 m and 0.7 m . In order to provide this spectral efficiency, uncoded SM operates with a signal constellation size of $M = 1$, i.e. all bits to be transmitted are conveyed in the spatial domain because $R = \log_2(N_t)$. In contrast, TCSM has to operate with $M = 2$ to compensate for the redundancy induced by the encoder. Moreover, the enhanced coded SM scheme has to operate with an even larger constellation size of $M = 4$ to provide the same data rate. As shown, despite this enlarged signal constellation size, our enhanced coded SM scheme can achieve gains in signal to noise ratio (SNR) of about $2 - 3 \text{ dB}$ compared to TCSM and outperforms uncoded SM by about $6 - 10 \text{ dB}$. Moreover, it can be seen that an enlargement of the transmitter spacing,

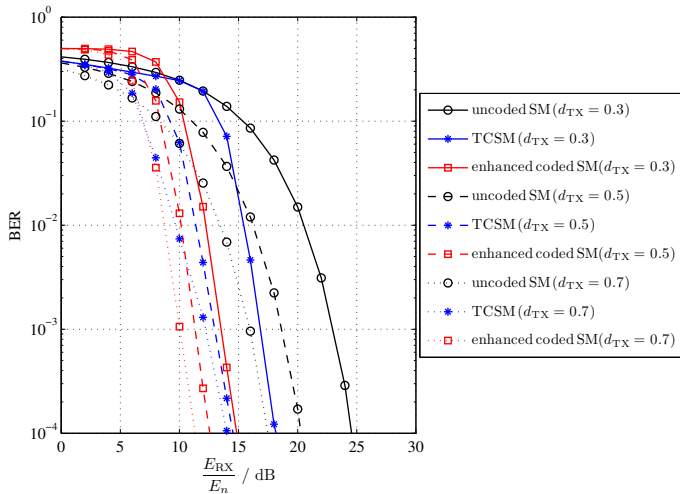


Fig. 6. BER of coded and uncoded SM for spectral efficiency of $R = 2$ bit/s/Hz in 4×4 setup scenario with varying distance d_{TX} of transmitters on the x - and y -axis.

d_{TX} , increases the channel distinctness and improves the BER performance of both coded and uncoded SM. Fig. 7 displays the BER of the considered schemes for $R = 3$ bit/s/Hz. In this scenario, uncoded SM operates with a signal constellation size of $M = 2$ and TCSM with $M = 4$. The enhanced coded SM scheme has to operate with $M = 16$. As depicted, the new enhanced coded SM scheme can also outperform both other schemes for $R = 3$ bit/s/Hz and achieves SNR gains of about 1 – 2 dB compared to TCSM, respectively of about 4 – 8 dB compared to uncoded SM, despite the fact that it has to use a much larger signal constellation size to compensate for the induced FEC coding.

V. SUMMARY AND CONCLUSION

In this paper, we have studied the performance of coded SM applied to OWC in indoor environments. It has been shown that FEC coding can significantly improve the performance of SM under conditions with high link correlation and low channel distinctness. Moreover, we have proposed an enhanced coded SM scheme which jointly encodes the bits conveyed in the spatial and signal domains. It has been found in this paper that our approach can outperform the originally proposed TCSM scheme by several dB. This is because the jointly encoding conveys the coded bits in the spatial as well as in the signal domain. As a consequence, our enhanced coded SM scheme can make better use of the basic SM detection principle which jointly detects the emitter index and the transmitted signal by a common operation. Consequently, our enhanced coded SM scheme utilises the output of the ML detector more efficiently than the originally proposed TCSM scheme, thus providing larger coding gains. Future work might deal with the performance of coded SM for higher spectral efficiencies and different coding rates as well as its evaluation for outdoor free space optical (FSO) communications employing laser diodes.

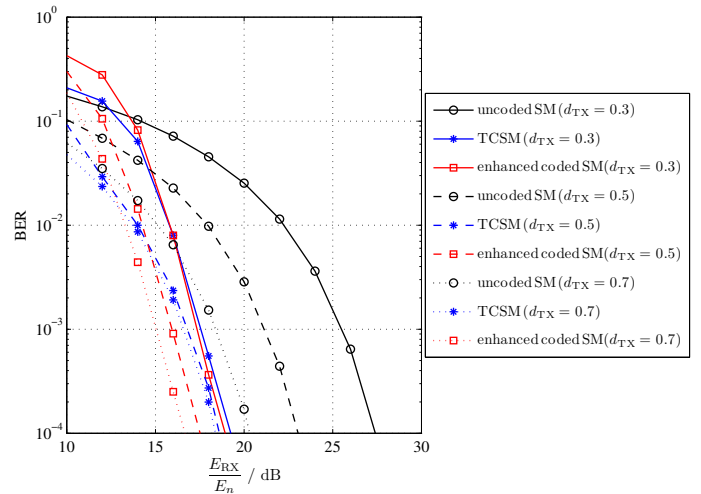


Fig. 7. BER of coded and uncoded SM for spectral efficiency of $R = 3$ bit/s/Hz in 4×4 setup scenario with varying distance d_{TX} of transmitters on the x - and y -axis.

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